# Assignment #2: Poisson Surface Reconstruction

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https://qingfang1208.github.io/

### Indicator Function

Reconstruct the surface by solving for the indicator function of the shape

$$\chi_M(p) = \begin{cases} 1, \text{ if } p \in M \\ 0, \text{ if } p \notin M \end{cases}$$

> How to construct the indicator function?



# Gradient Relationship

There is a relationship between the normal field and gradient of indicator function



#### Integration as a Poisson Problem

- > Represent the points by a vector field  $\vec{V}$
- > Find the function  $\chi$  whose gradient best approximates  $\vec{V}$

$$\min_{\chi} \|\nabla \chi - \vec{V}\|^2$$

> Applying the divergence operator, we can transform this into a Poisson problem

$$abla \cdot (\nabla \chi) = \nabla \cdot \vec{V} \implies \Delta \chi = \nabla \cdot \vec{V}$$

- > Given the Points:
  - Set Octree
  - Compute vector field
  - Compute indicator function
  - Extract iso-surface



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# Summary

#### Paper: Kazhdan et al. 2006 Poisson Surface Reconstruction



#### Assignment requirements

> Email: ID\_name\_homework#2\_(win or mac ).zip

- Pdf : Input + parameter + output
- Source code (no exe)
- Deadline: 2024.03.24, 23:59